

Amendments to the Claims:

This listing of claims will replace all prior versions, and listings, of claims in the application.

Listing of Claims:

1. (Previously Presented) An asymmetrical key cryptography method involving a keyholder having a number $m \geq 1$ of private keys Q_1, Q_2, \dots, Q_m and respective public keys G_1, G_2, \dots, G_m , each pair of keys (Q_i, G_i) (where $i = 1, \dots, m$) satisfying either the relationship $G_i = Q_i^v \bmod n$ or the relationship $G_i \times Q_i^v = 1 \bmod n$, where n is a public integer equal to the product of f (where $f > 1$) private prime factors p_1, \dots, p_f , at least two of which are separate, and the exponent v is a public integer equal to a power of 2, wherein the method comprises the steps of:

arranging exponent v to have the relationship $v = 2^{b+k}$,

where k is a strictly positive integer and $b = \max(b_1, \dots, b_f)$, where b_j (where $j = 1, \dots, f$) is the highest integer such that $(p_j - 1) / 2^{b_j - 1}$ is even; $[[.]]$ and

arranging each public key G_i (where $i = 1, \dots, m$) to have the form $G_i = g_i^{2^{a_i}} \bmod n$,

where the base numbers g_i are integers strictly greater than 1 and the numbers a_i are integers such that $1 \leq a_i \leq b$ and at least one of them is strictly greater than 1.

2. (Previously Presented) A method according to claim 1, wherein at least one of said prime factors p_1, \dots, p_f is congruent to 1 modulo 4 and the integers a_i (where $i = 1, \dots, m$) are all equal to said number b .

3. (Previously Presented) A method according to claim 1, wherein said base numbers g_1, \dots, g_m include at least one number g_s and said prime factors p_1, \dots, p_f include at least two numbers p_t and p_u other than 2 such that, given said numbers b_1, \dots, b_f ,

if $b_t = b_u$, then $(g_s | p_t) = -(g_s | p_u)$, and

if $b_t < b_u$, then $(g_s | p_u) = -1$,

where $(g_s | p_t)$ and $(g_s | p_u)$ denote the Legendre symbols of g_s relative to p_t and p_u .

4. (Previously Presented) A method according to claim 1, wherein the base numbers g_1, \dots, g_m are prime numbers.

5. (Previously Presented) A method according to claim 1, involving a controller and said keyholder, here called the claimant, wherein the method comprises the following steps:

the claimant chooses at random an integer r , calculates the witness $R = r^v \bmod n$ and sends the witness to the controller,

the controller chooses at random m challenges d_1, d_2, \dots, d_m and sends the challenges to the claimant,

the claimant calculates the response

$$D = r \times Q_1^{d_1} \times Q_2^{d_2} \times \dots \times Q_m^{d_m} \bmod n,$$

and sends the response to the controller, and

the controller calculates

$$D^v \times G_1^{e_1 d_1} \times G_2^{e_2 d_2} \times \dots \times G_m^{e_m d_m} \bmod n$$

where, for $i = 1, \dots, m$, $\varepsilon_i = +1$ if $G_i \times Q_i^v = 1 \bmod n$ and $\varepsilon_i = -1$ if $G_i = Q_i^v \bmod n$,

and verifies that the result is equal to the witness R .

6. (Previously presented) A method according to claim 1, enabling a controller to verify that a message M that it has received was sent to it by said keyholder, here called the claimant, wherein the method comprises the following steps:

the claimant chooses at random an integer r and first calculates the witness $R = r^v \bmod n$, then calculates the token $T = h(M, R)$, where h is a hashing function, and finally sends the token T to the controller,

the controller chooses at random m challenges d_1, d_2, \dots, d_m , and sends the challenges to the claimant,

the claimant calculates the response

$D = r \times Q_1^{d_1} \times Q_2^{d_2} \times \dots \times Q_m^{d_m} \bmod n$ and sends the response to the controller, and

the controller calculates $h(M, D^v \times G_1^{\varepsilon_1 d_1} \times G_2^{\varepsilon_2 d_2} \times \dots \times G_m^{\varepsilon_m d_m} \bmod n)$ where, for $i = 1, \dots, m$, $\varepsilon_i = +1$ if $G_i \times Q_i^v = 1 \bmod n$ and $\varepsilon_i = -1$ if $G_i = Q_i^v \bmod n$, and verifies that the result is equal to the token T .

7. (Previously presented) A method according to claim 5, wherein the challenges satisfy the condition $0 \leq d_i \leq 2^k - 1$ for $i = 1, \dots, m$.

8. (Previously presented) A method according to claim 1, enabling said keyholder, here called the signatory, to sign a message M that it sends to a controller, wherein the method comprises the following steps:

the signatory chooses at random m integers r_i , where $i = 1, \dots, m$, and first calculates the witnesses $\underline{R_i = r_i^v \bmod n}$, then calculates the token $T = h(M, R_1, R_2, \dots, R_m)$, where h is a hashing function producing a word of m bits, and finally sends the token T to the controller,

the signatory identifies the bits d_1, d_2, \dots, d_m of the token T ,

the signatory calculates the responses $D_i = r_i \times Q_i^{d_i} \bmod n$ and sends the responses to the controller, and

the controller calculates

$$h \left(M, D_1^v \times G_1^{\varepsilon_1 d_1} \bmod n, D_2^v \times G_2^{\varepsilon_2 d_2} \bmod n, \dots, D_m^v \times G_m^{\varepsilon_m d_m} \bmod n \right)$$

where, for $i = 1, \dots, m$, $\varepsilon_i = +1$ if $G_i \times Q_i^v = 1 \bmod n$ and $\varepsilon_i = -1$ if $G_i = Q_i^v \bmod n$, and verifies that the result is equal to the token T .

9. (Previously presented) An electronic circuit including a processor and memories, wherein the electronic circuit is programmed to act as said keyholder in executing a method according to claim 1.

10. (Previously Presented) A dedicated electronic circuit, including microcomponents enabling the electronic circuit to process data in such manner as to act as said keyholder in executing a method according to claim 1.

11. (Previously presented) A portable object adapted to be connected to a terminal to exchange data with that terminal, wherein the portable object includes an electronic circuit according to claim 9 or claim 10 and is adapted to store identification data and private keys specific to said key holder.

12. (Previously presented) A terminal adapted to be connected to a portable object to exchange data with that portable object, wherein the terminal includes a data processing device programmed to act as said controller in executing a method according to any one of claims 5-8.

13. (Previously presented) A cryptography system comprising:
a portable object adapted to be connected to a terminal to exchange data with that terminal, wherein the portable object includes an electronic circuit,

wherein the electronic circuit is programmed to act as said keyholder in executing an asymmetrical key cryptography method involving a keyholder having a number $m \geq 1$ of private keys Q_1, Q_2, \dots, Q_m and respective public keys G_1, G_2, \dots, G_m , each pair of keys (Q_i, G_i) (where $i = 1, \dots, m$) satisfying either the relationship $G_i = Q_i^v \bmod n$ or the relationship $G_i \times Q_i^v = 1 \bmod n$, where n is a public integer equal to the product of f (where $f > 1$) private prime factors p_1, \dots, p_f , at least two of which are separate, and the exponent v is a public integer equal to a power of 2, wherein the method comprises the steps of:

arranging exponent v to have the relationship $v = 2^{b+k}$,

where k is a strictly positive integer and $b = \max(b_1, \dots, b_f)$, where b_j (where $j = 1, \dots, f$) is the highest integer such that $(p_j - 1)/2^{b_j - 1}$ is even; and

arranging each public key G_i (where $i = 1, \dots, m$) to have the form

$$G_i = g_i^{2^{b_i}} \bmod n,$$

where the base numbers g_i are integers strictly greater than 1 and the numbers a_i are integers such that $1 \leq a_i \leq b$ and at least one of them is strictly greater than 1,

and wherein the portable object is adapted to store identification data and private keys specific to said key holder; and

a terminal adapted to be connected to the portable object to exchange data with that portable object, wherein the terminal includes a data processing device programmed to act as said controller in executing a method according to any one of claims 5-8.

14. (Previously Presented) Non-removable data storage means containing electronic data processing program code instructions for, as said keyholder, executing the steps of a method according to claim 1.

15. (Previously Presented) Partially or totally removable storage means containing electronic data processing program code instructions for, as said keyholder, executing the steps of a method according to claim 1.

16. (Previously presented) A data processing device comprising storage means according to claim 14 or claim 15.

17. (Currently amended) Non-removable, partially removable, or totally removable data storage means containing electronic data processing program code instructions for, as said controller, executing the steps of a method according to any one of claims 5-8.

18. (Canceled)

19. (Currently Amended) A data processing device, wherein it comprises storage means according to claim 17 ~~or claim 18~~.

20. (Previously presented) A cryptography system comprising:
a data processing device including storage means containing electronic data processing program code instructions for, as said keyholder, executing the steps of an asymmetrical key cryptography method involving a keyholder having a number $m \geq 1$ of private keys Q_1, Q_2, \dots, Q_m and respective public keys G_1, G_2, \dots, G_m , each pair of keys (Q_i, G_i) (where $i = 1, \dots, m$) satisfying either the relationship $G_i = Q_i^v \bmod n$ or the relationship $G_i \times Q_i^v = 1 \bmod n$, where n is a public integer equal to the product of f (where $f > 1$) private prime factors p_1, \dots, p_f , at least two of which are separate, and the exponent v is a public integer equal to a power of 2, wherein the method comprises the steps of:

arranging exponent v to have the relationship $v = 2^{b+k}$,

where k is a strictly positive integer and $b = \max(b_1, \dots, b_f)$, where b_j (where $j = 1, \dots, f$) is the highest integer such that $(p_j - 1) / 2^{b_j - 1}$ is even; and

arranging each public key G_i (where $i = 1, \dots, m$) to have the form

$$G_i = g_i^{2^{a_i}} \bmod n,$$

where the base numbers g_i are integers strictly greater than 1 and the numbers a_i are integers such that $1 \leq a_i \leq b$ and at least one of them is strictly greater than 1; and

a data processing device including data storage means containing electronic data processing program code instructions for, as said controller, executing the steps of a method according to any one of claims 5-8.

21. (Canceled).

22. (Previously Presented) A method according to claim 4, wherein the base numbers g_1, \dots, g_m are chosen from the first 54 prime numbers.